

**Universität zu Köln**

Seminar für Allgemeine Betriebswirtschaftslehre, Supply Chain Management und Management Science

# **Optimizing Crew Schedules with Fairness Preferences**

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- ➔ ■ **Problem Description**
- Mathematical Model
- Computational Results

# THE FREIGHT RAILWAY CREW SCHEDULING PROBLEM



## Freight Transport

- Trains operate between stations on a given timetable
- Trains segmented into trips (i.e., movements serviced by same driver)



## Crew

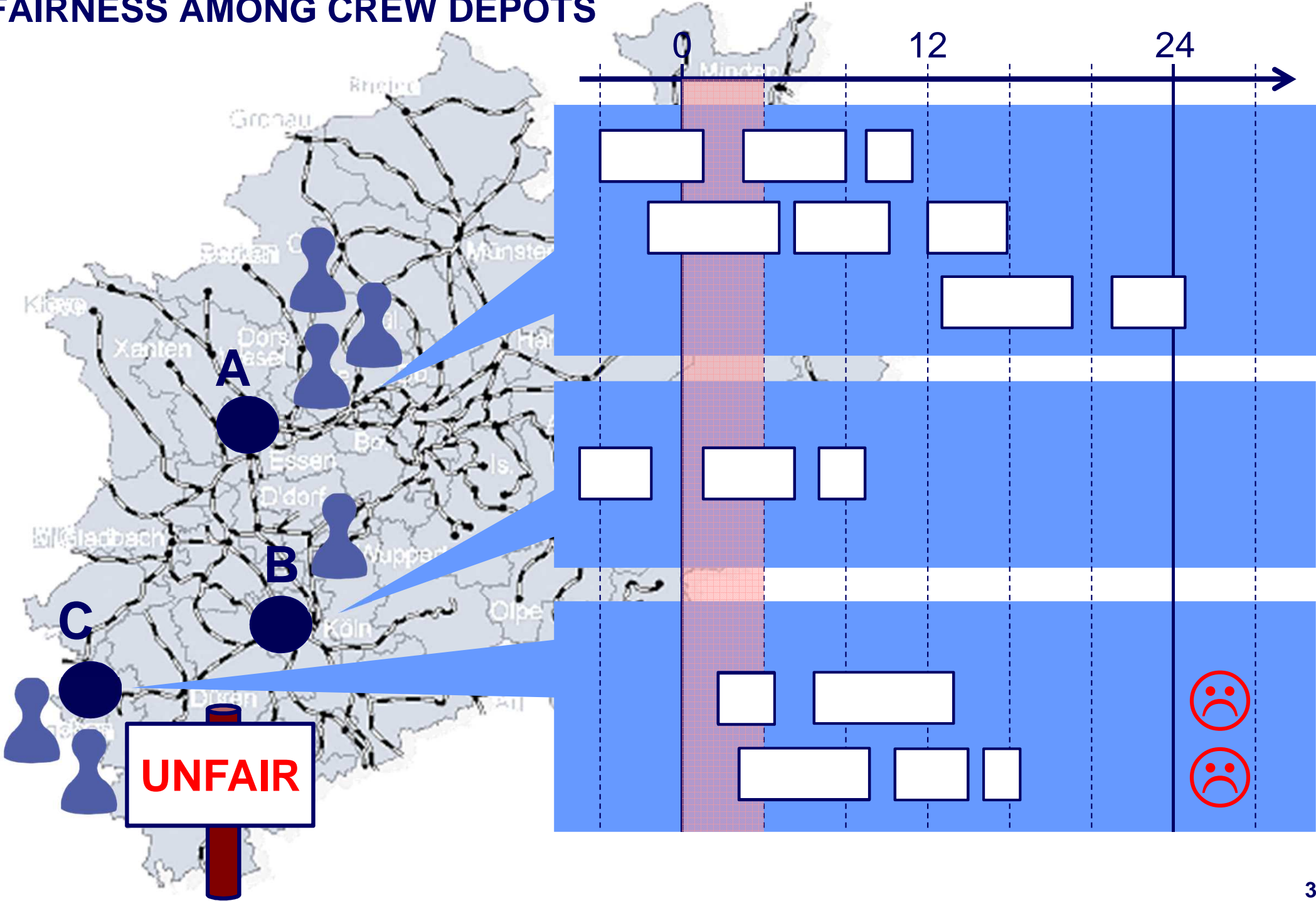
- Drivers needed to run locomotives
- Operational and contractual requirements
- Crew capacity limits at depots

## Railway Crew Scheduling Problem:

Build driver duties from trips such that

- all trips are covered
- all work regulations are met
- capacity limits are respected
- overall costs are minimized

# FAIRNESS AMONG CREW DEPOTS



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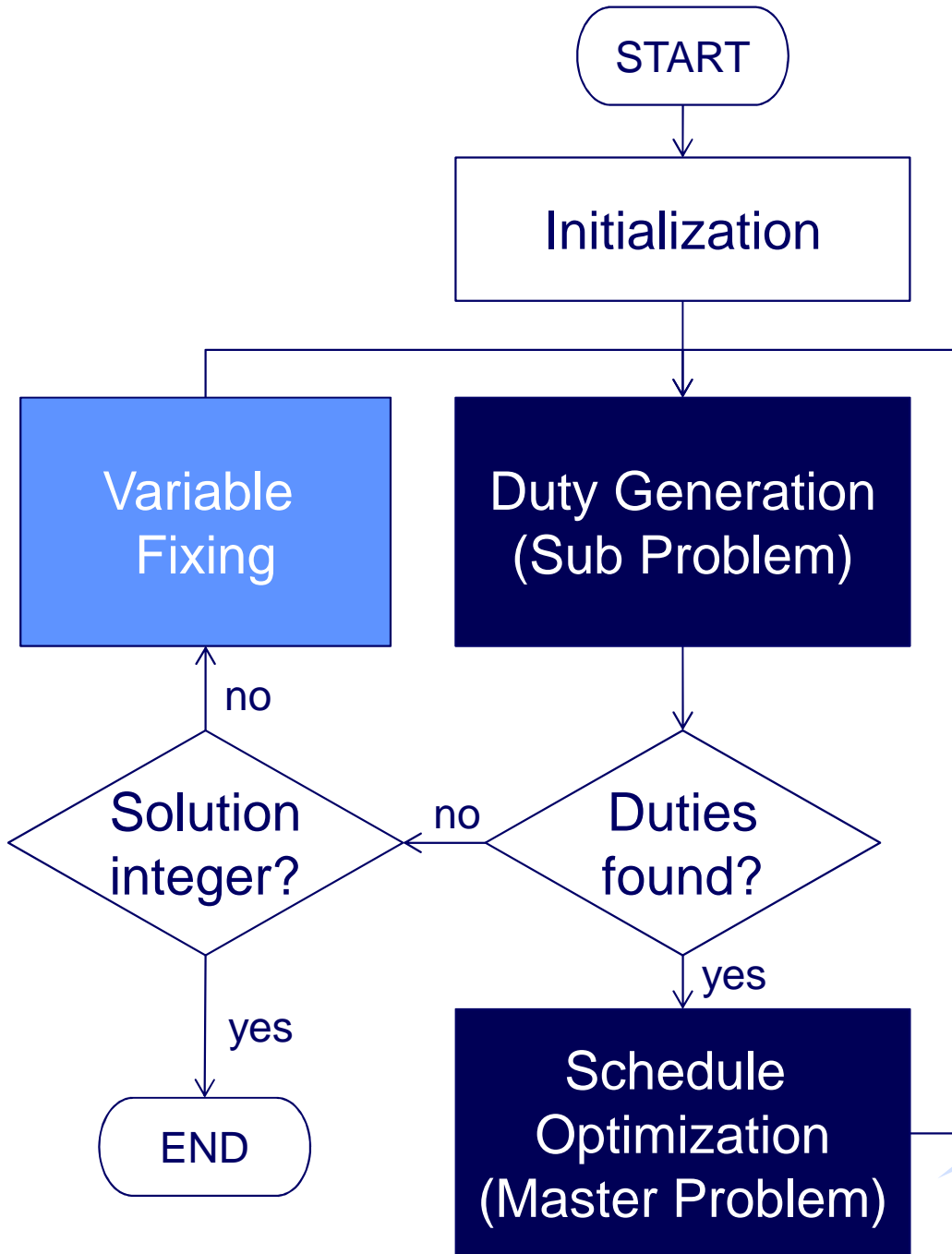
- Problem Description

- ➔ ■ **Mathematical Model**

- Computational Results

# MATHEMATICAL MODEL: BASIS

$d \in D$     duties  
 $j \in J$     depots  
 $t \in T$     trips



$$\begin{aligned}
 \min z &= \sum_{d \in D} c_d x_d + \sum_{j \in J} \hat{c}_j \hat{y}_j \\
 \text{s.t.} \\
 \sum_{d \in D} a_{td} x_d &\geq 1 \quad \forall t \in T \\
 \sum_{j \in J} b_{jd} x_d - \hat{y}_j &\leq k_j \quad \forall j \in J \\
 x_d, \hat{y}_j &\geq 0 \quad \forall d \in D, j \in J
 \end{aligned}$$

# MATHEMATICAL MODEL: INCLUDING FAIRNESS

$$\min z = \sum_{d \in D} c_d x_d + \sum_{j \in J} \hat{c}_j \hat{y}_j + \sum_{j \in J} k_j \tilde{c}_j \tilde{y}_j$$

s.t.

Schedule  
unfairness

$$F = \sum_{j \in J} k_j (U_j - U)^+$$

Duty unpopularity

$u_d$

$$\sum_{d \in D} a_{td} x_d \geq 1 \quad \forall t \in T$$

$$\sum_{j \in J} b_{jd} x_d - \hat{y}_j \leq k_j \quad \forall j \in J$$

$$\frac{\sum_{d \in D} b_{jd} x_d u_d}{k_j} - \frac{\sum_{d \in D} x_d u_d}{\sum_{j \in J} k_j} - \tilde{y}_j \leq 0 \quad \forall j \in J$$

$$x_d, \hat{y}_j, \tilde{y}_j \geq 0 \quad \forall d \in D, j \in J$$

Depot unpopularity

$U_j$

Schedule unpopularity

$U$

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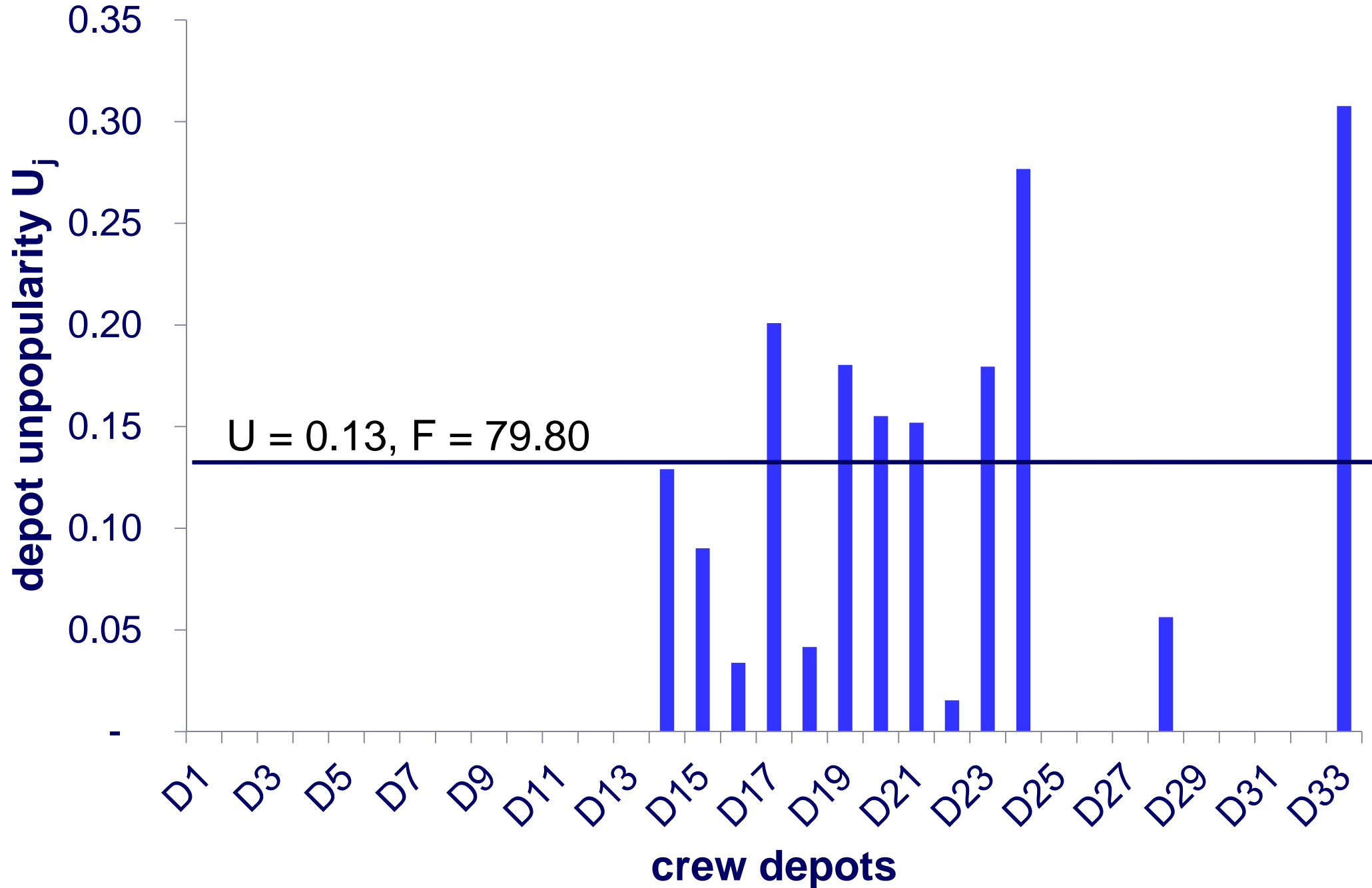
- Problem Description

- Mathematical Model

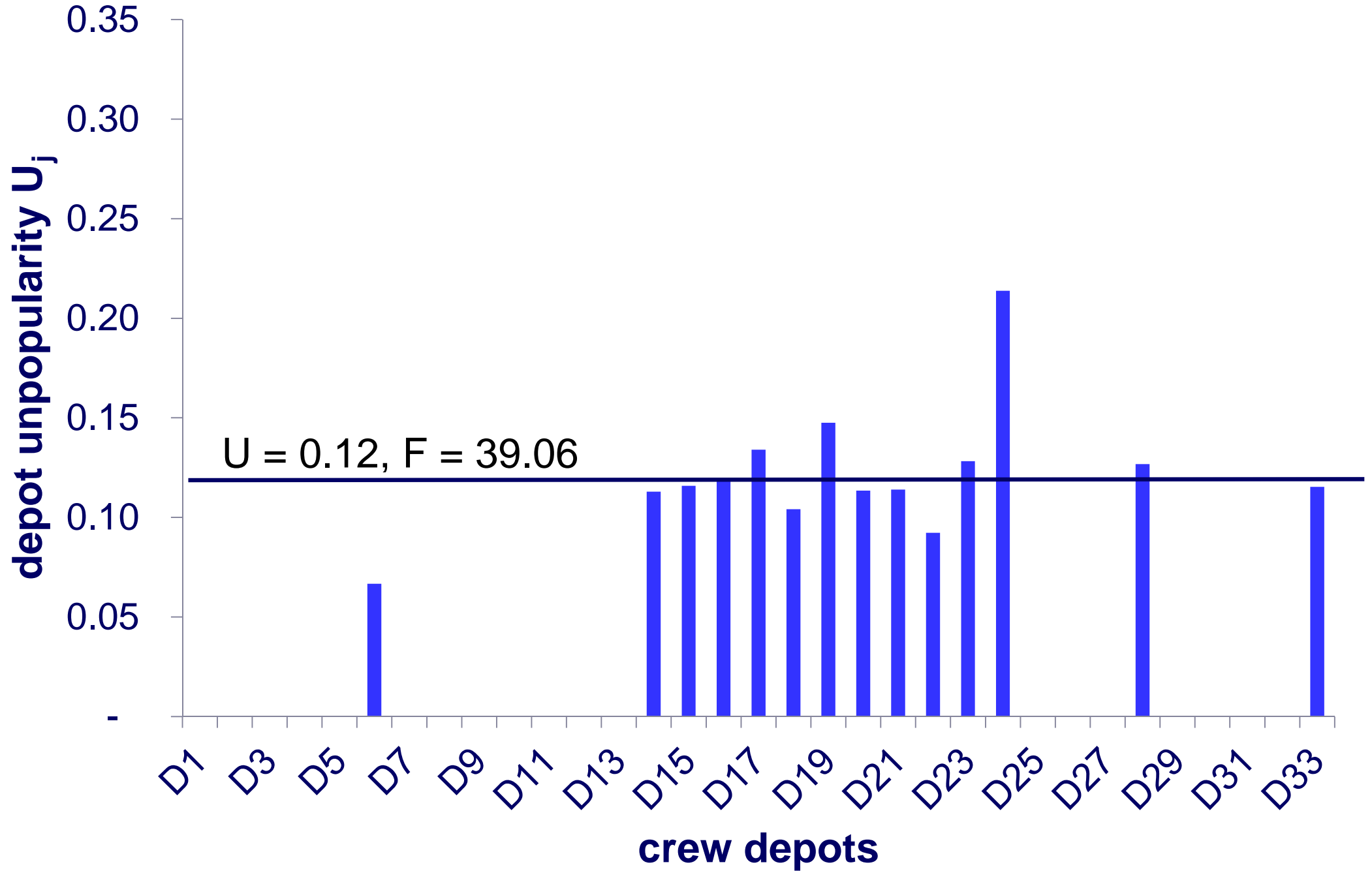
- ➔ ■ **Computational Results**



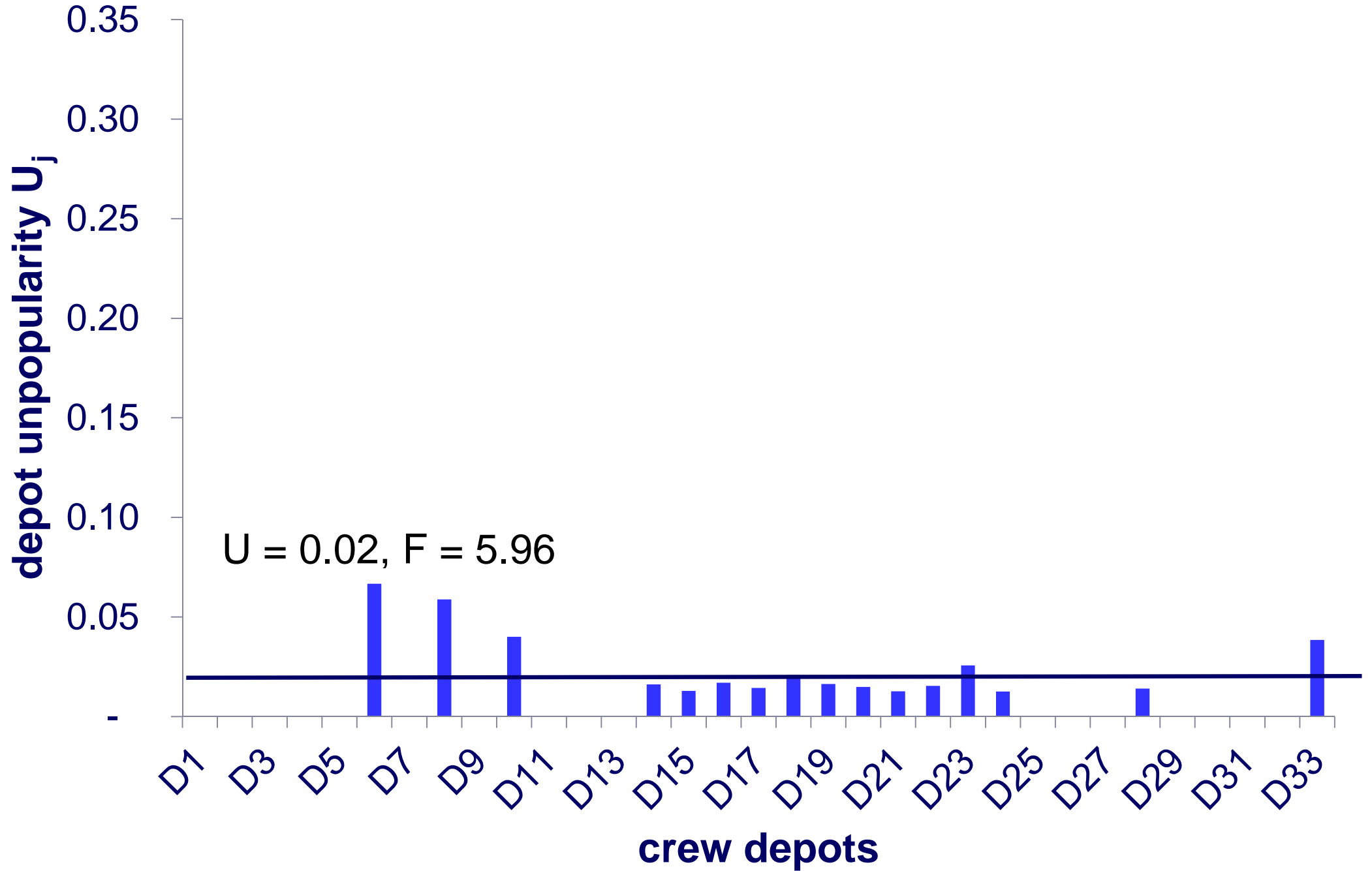
# SAMPLE RESULTS: CIRCADIAN RHYTHM (1/5)



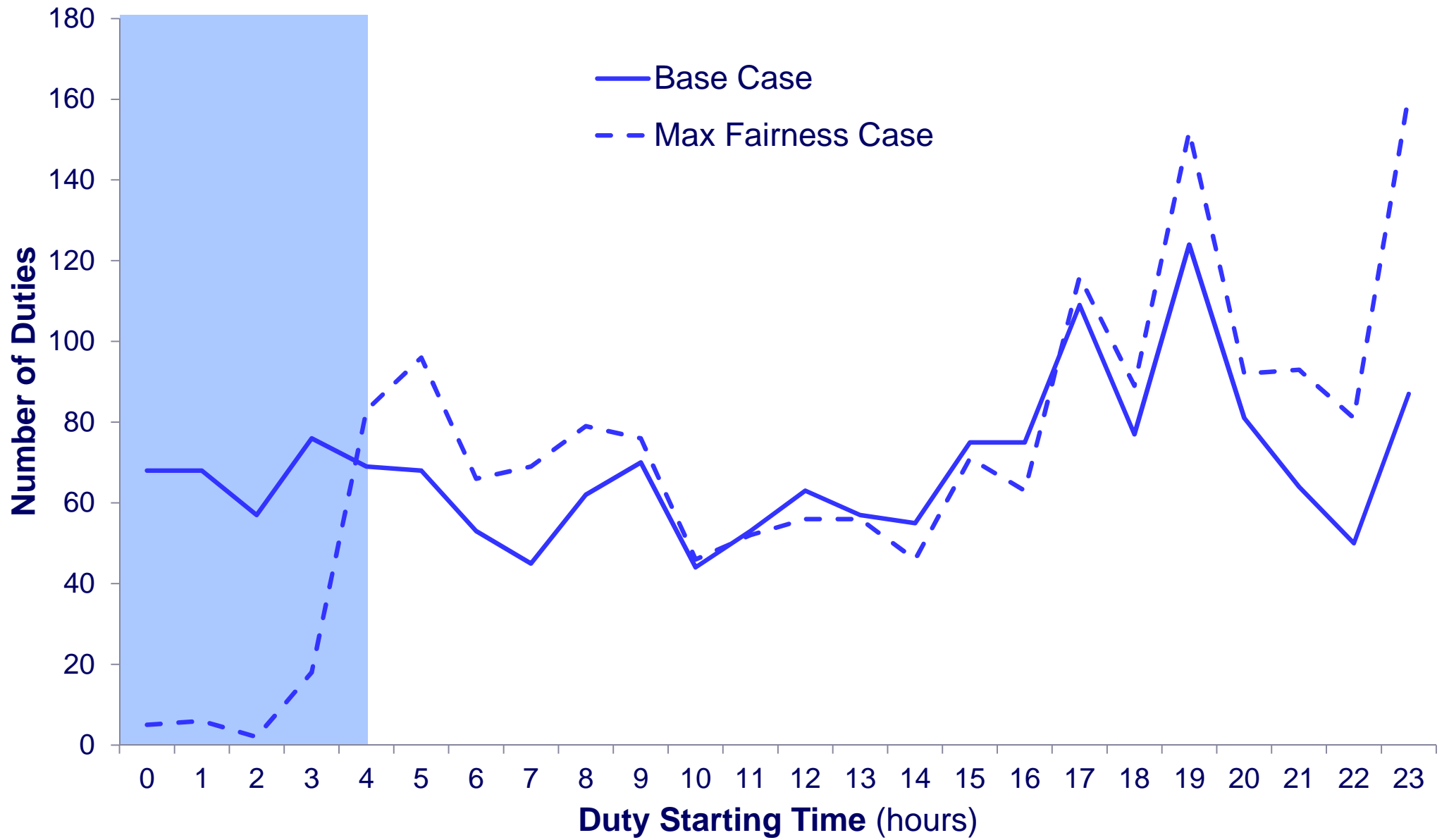
# SAMPLE RESULTS: CIRCADIAN RHYTHM (2/5)



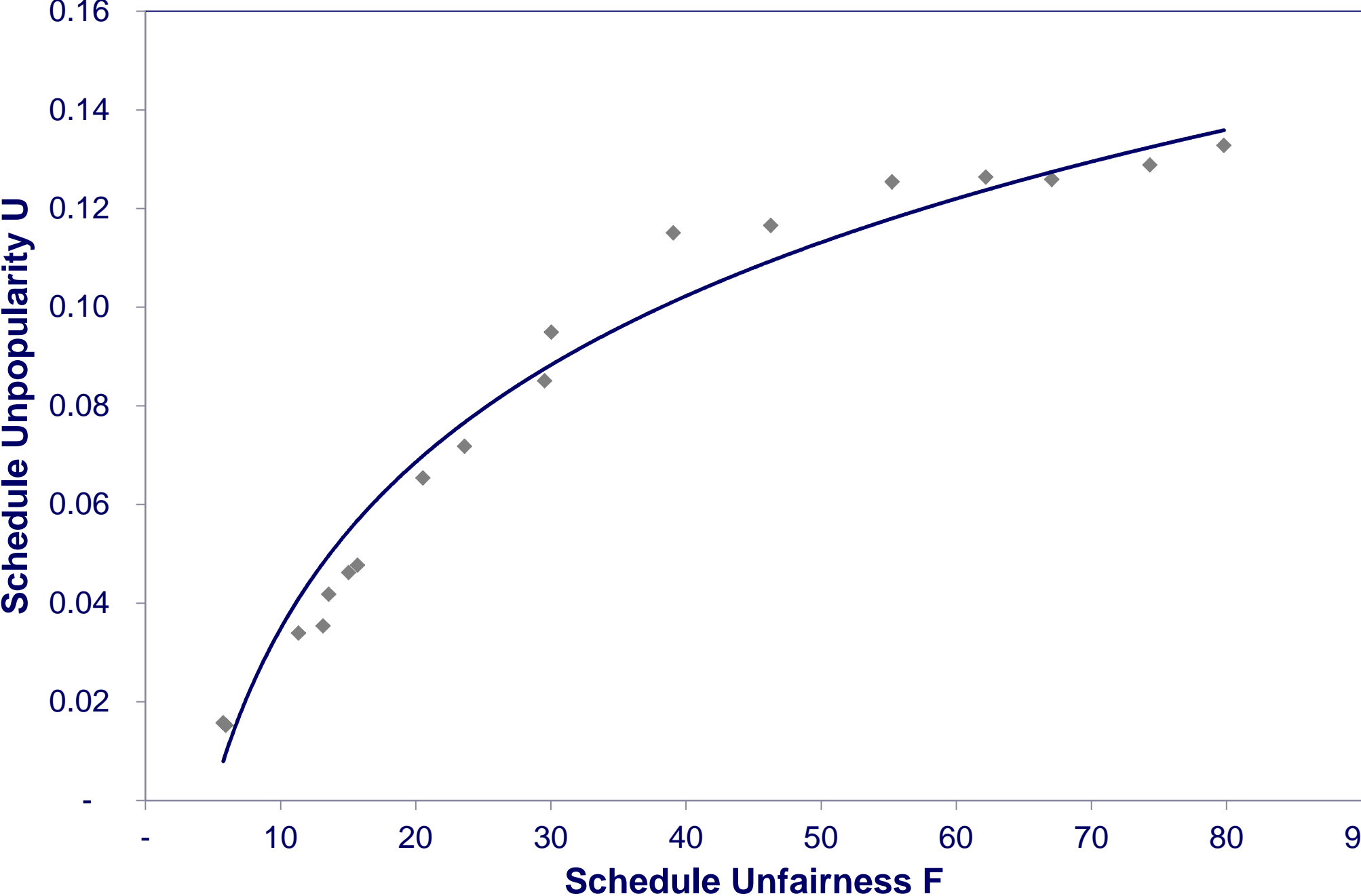
# SAMPLE RESULTS: CIRCADIAN RHYTHM (3/5)



# SAMPLE RESULTS: CIRCADIAN RHYTHM (4/5)

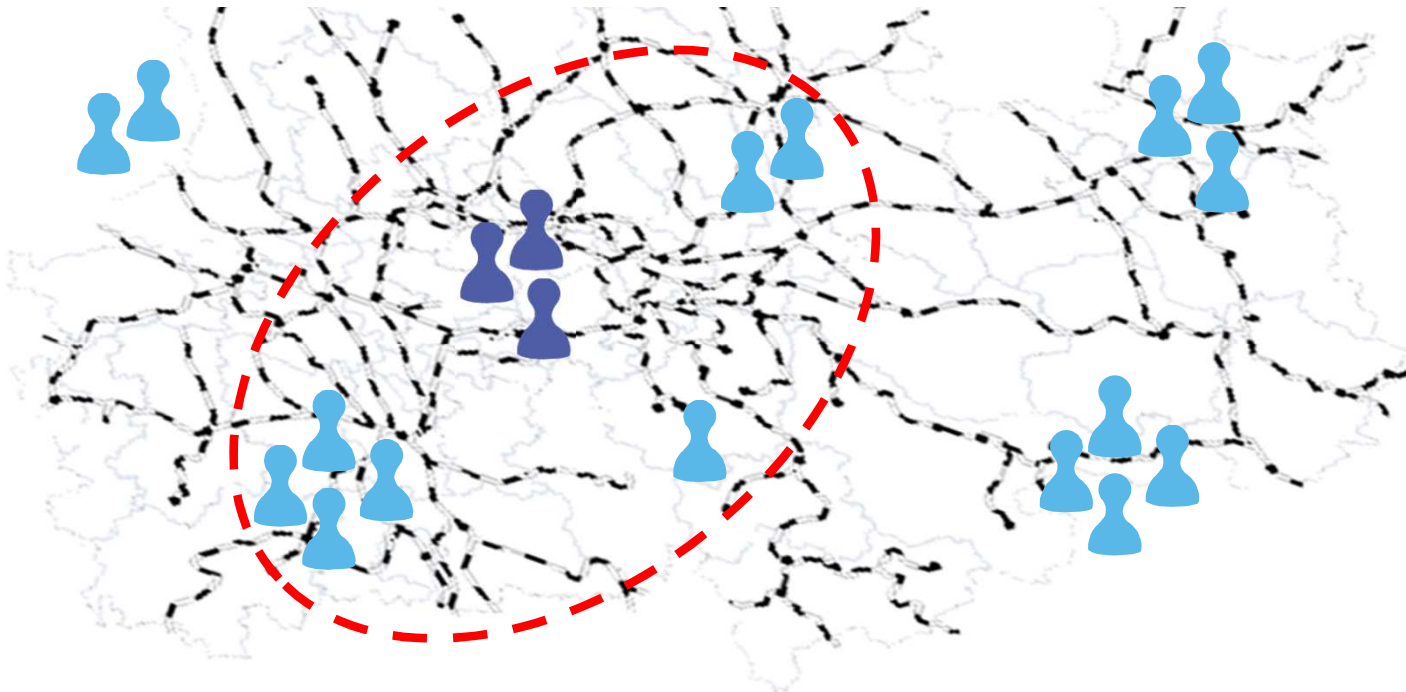


# SAMPLE RESULTS: CIRCADIAN RHYTHM (5/5)



# FUTURE RESEARCH INTERESTS

- **Fairness vs. unpopularity:** interdependence of fairness and unpopularity, comparison to pure unpopularity minimization, integration of unpopularity restrictions
- **Fairness perception:** include advantageous inequality, vary fairness perception among depots
- **Local fairness:** even distribution of unpopular properties within given geographical distances



Thank you for your attention.