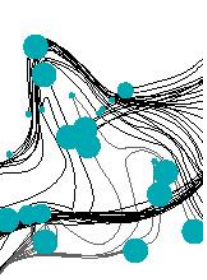




# The Pareto set as decision support information in multimodal passenger transportation network design

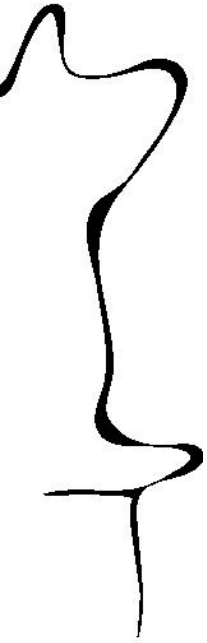
Ties Brands, Luc Wismans and Eric van Berkum





# Background

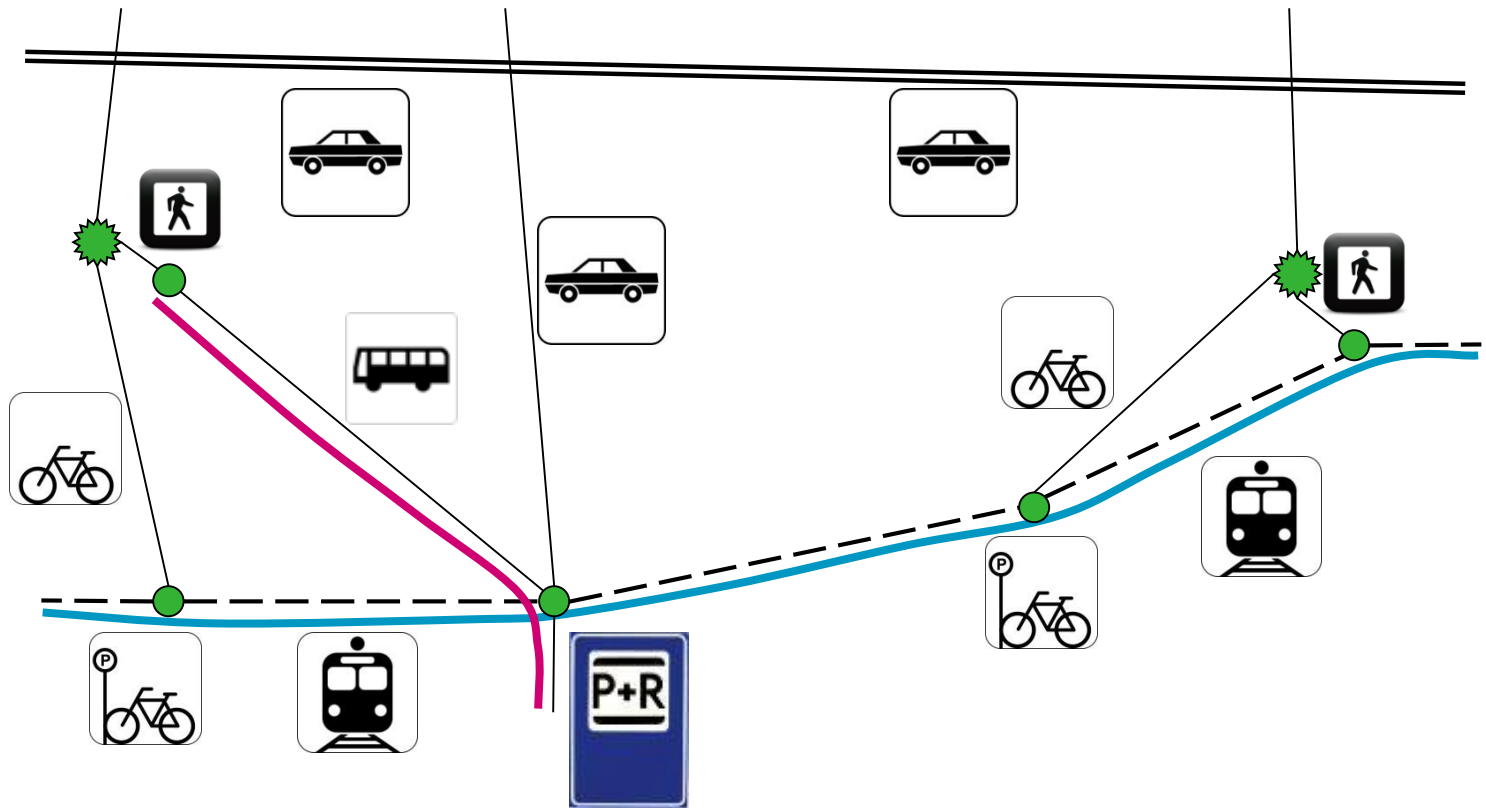
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- How to improve the passenger transportation network?
- What to improve: sustainability
  - → multi-objective is necessary for multiple aspects of sustainability
- How to improve: multimodal network improvements
- Optimisation: search for the best possible combination of measures
- → A lot of output
- Methods are needed to visualise and analyse the Pareto set



# Multimodal passenger transportation network





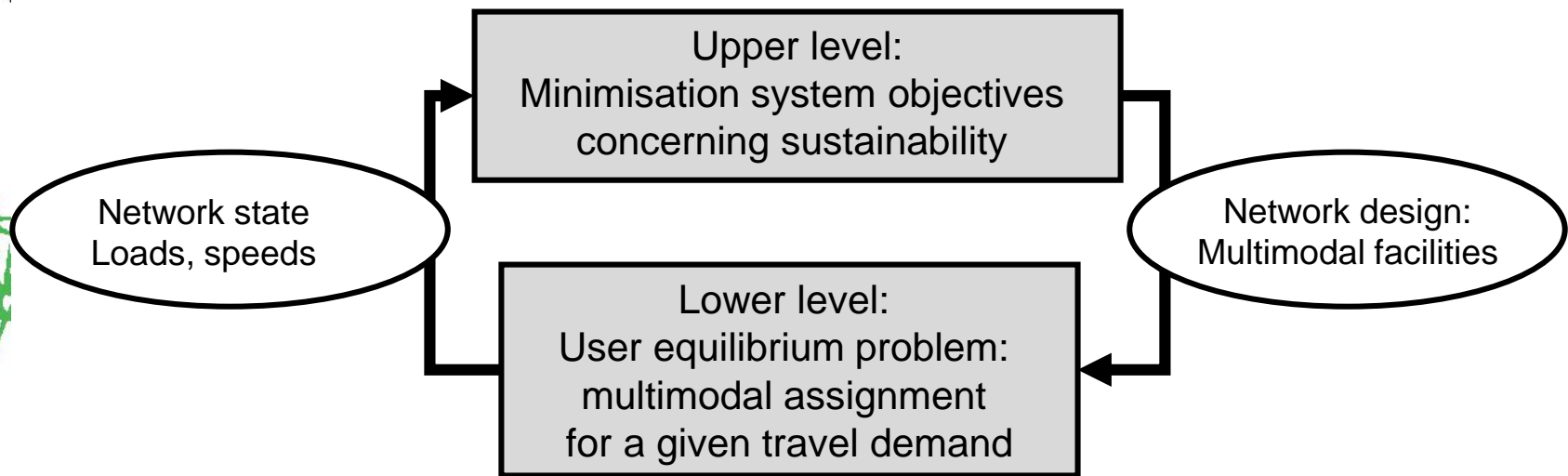
# Objective functions to be optimised

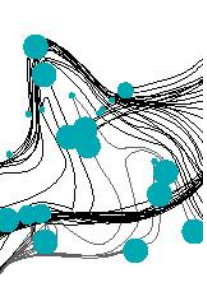
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Aspects of sustainability:

1. Accessibility: total travel time
2. Use of urban space by parking: car trips to and from urban areas
3. Operating deficit of public transportation (cost – revenue) and cost of park and ride
4. Climate impact: total CO<sub>2</sub> emissions for car and public transport vehicles

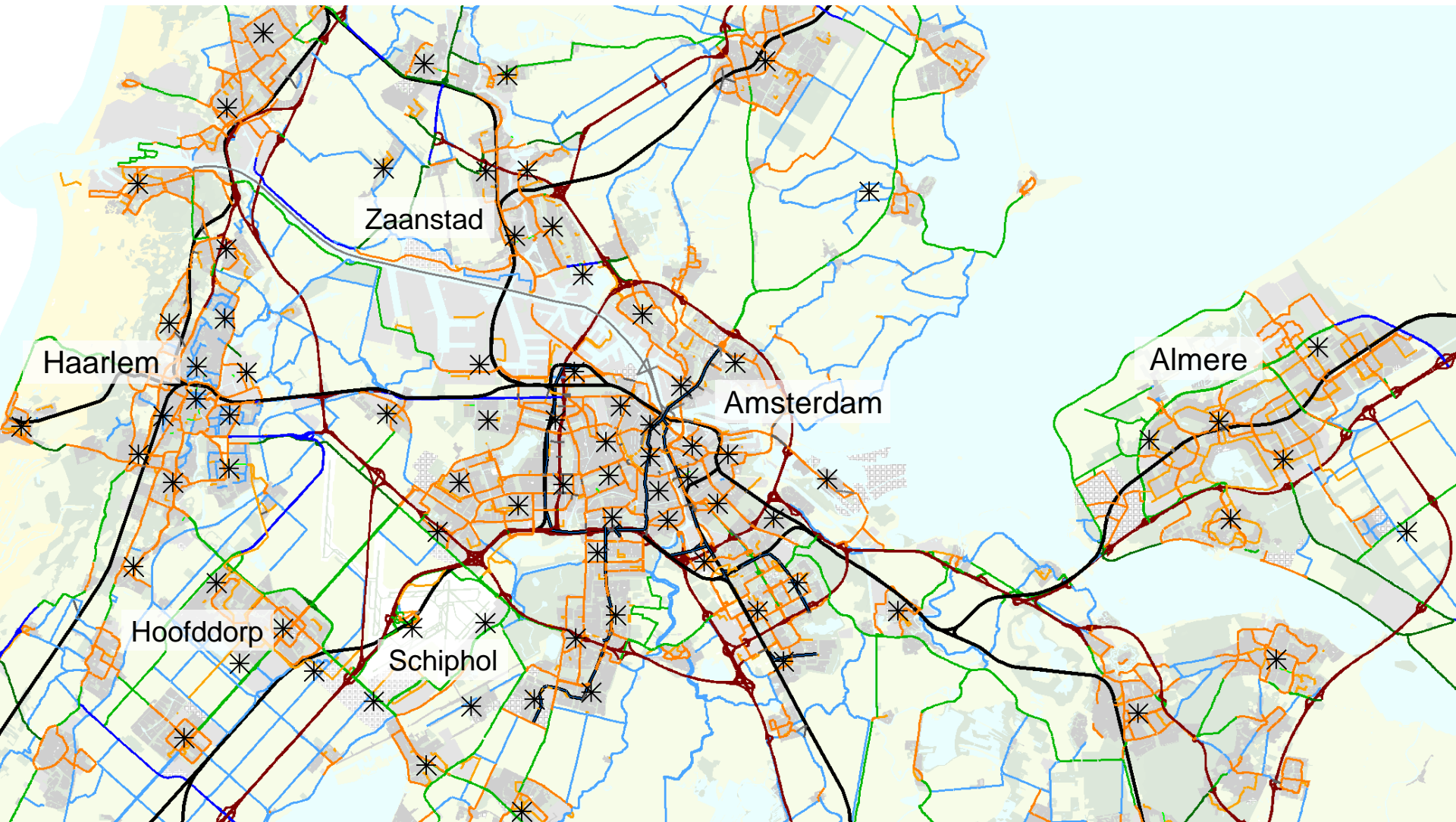
# Network design problem: bi-level optimisation

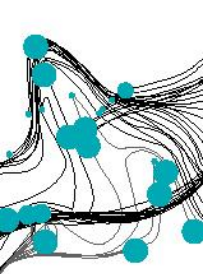




# Case study: Metropolitan region of Amsterdam in 2030

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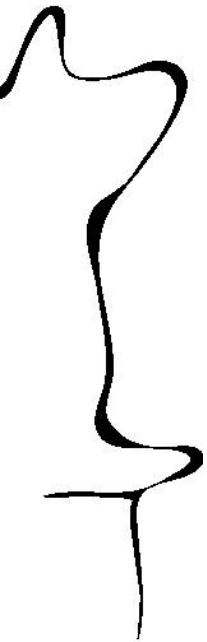




## 37 decision variables

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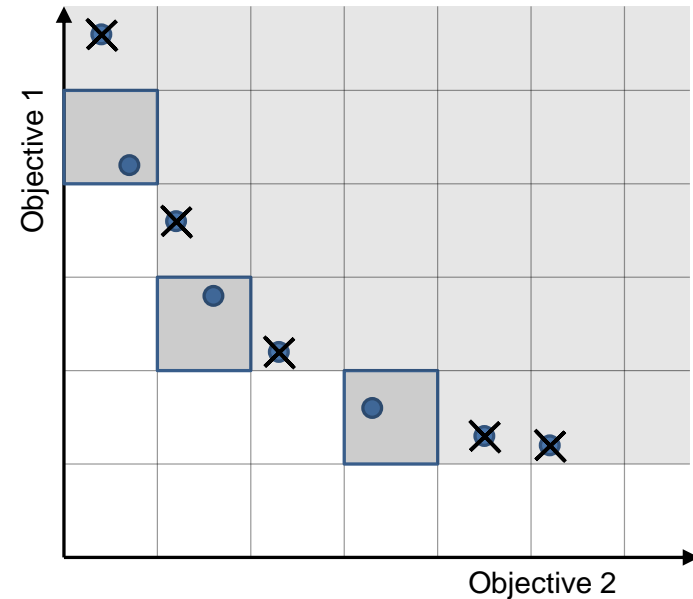
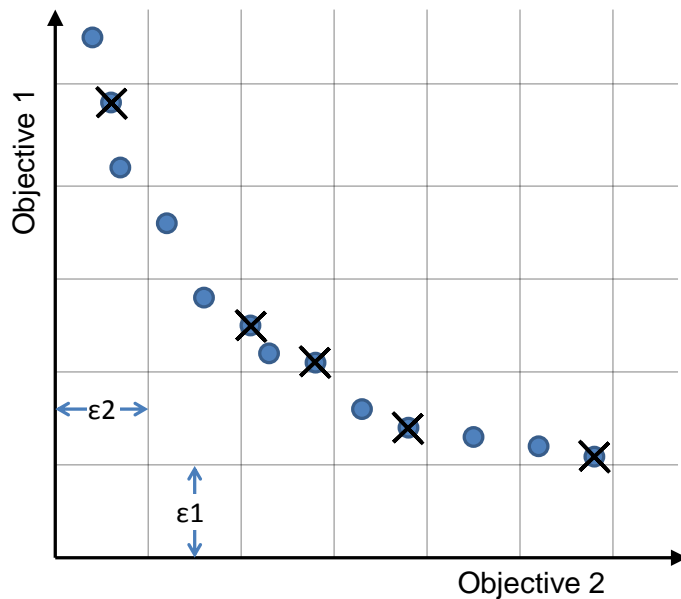
- 7 candidate locations for Park and Ride
- Frequency of 12 train lines
- Frequency of 8 bus lines
- 6 candidate locations for train stations
- 3 candidate locations for express train stations
- 1 possible tram line extension
- → Decision space contains  $7E13$  possible solutions
  
- Calculation time of 1 solution (running the lower level): 6 minutes



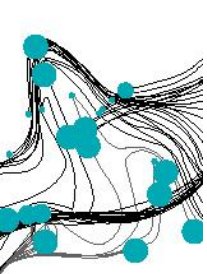


## Solution algorithm: $\epsilon$ -NSGAI

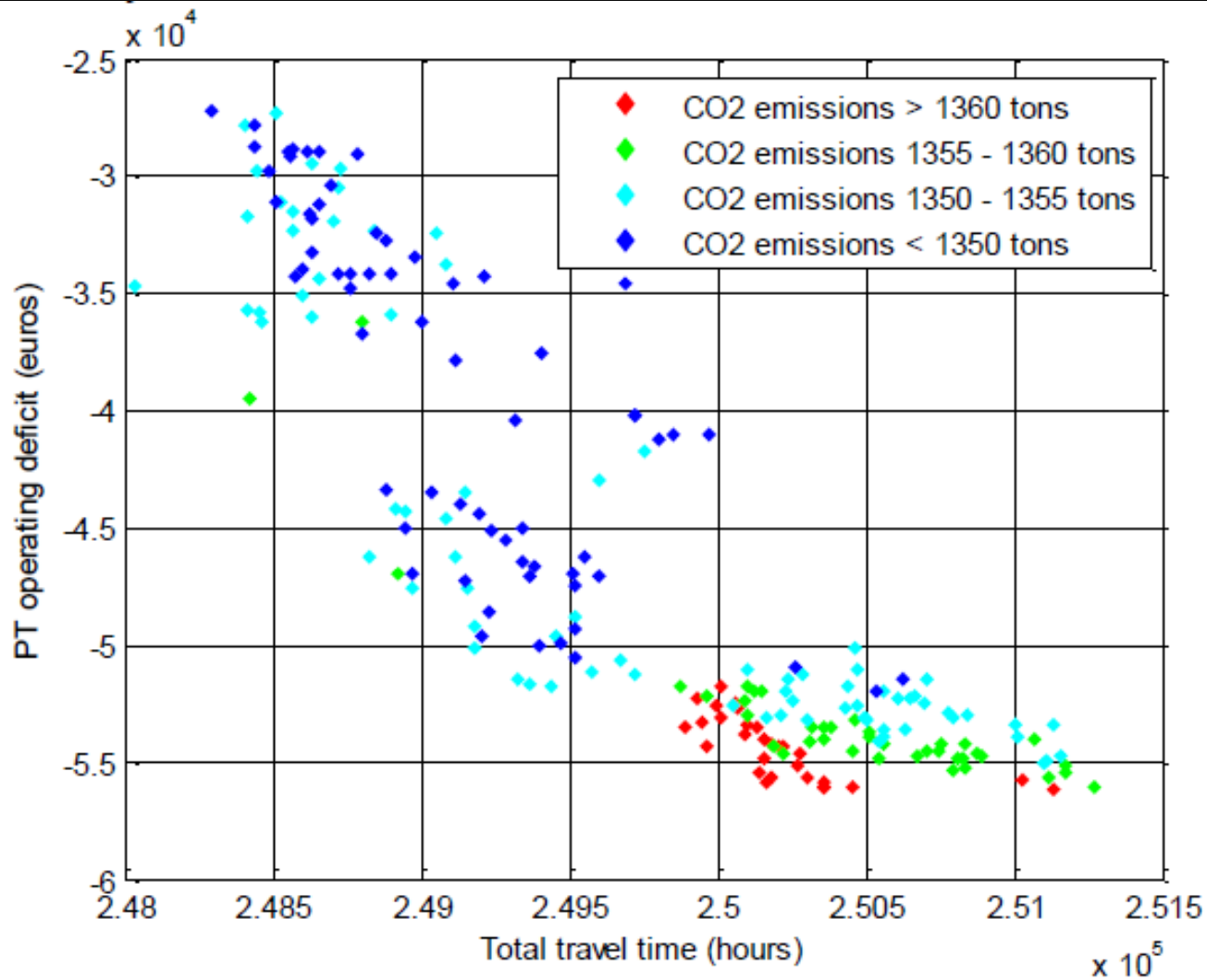
- Extension of well known genetic algorithm NSGAI
- $\epsilon$ -dominance to detect large progress over little progress
- No waste of calculation time when only little progress is made

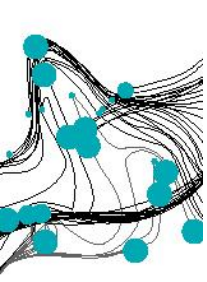




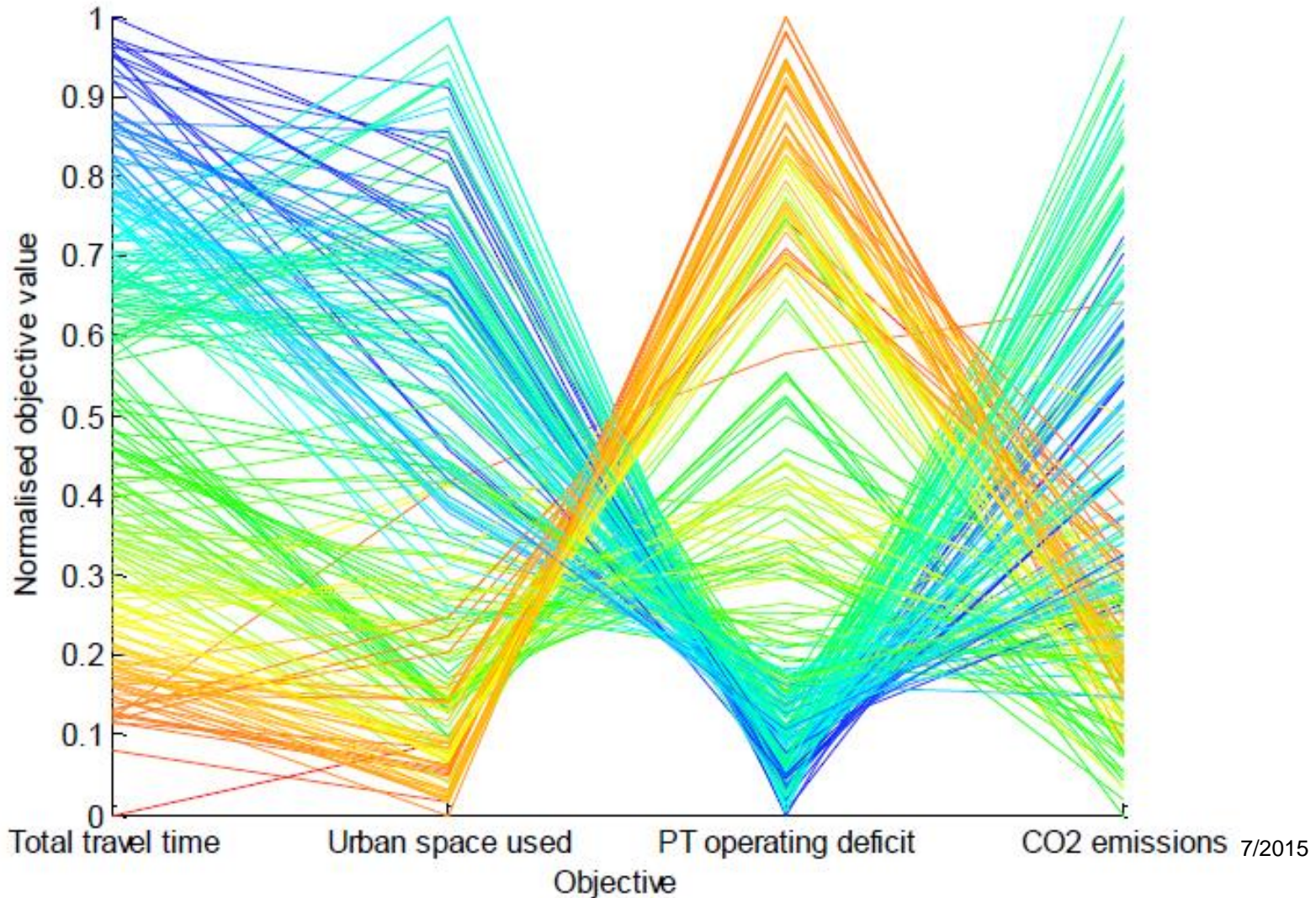


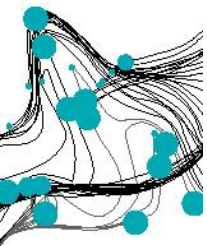
## Visualisation of the Pareto set: scatter plot



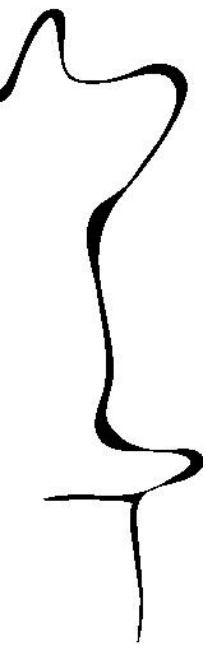


## Visualisation of the Pareto set: parallel coordinate plot

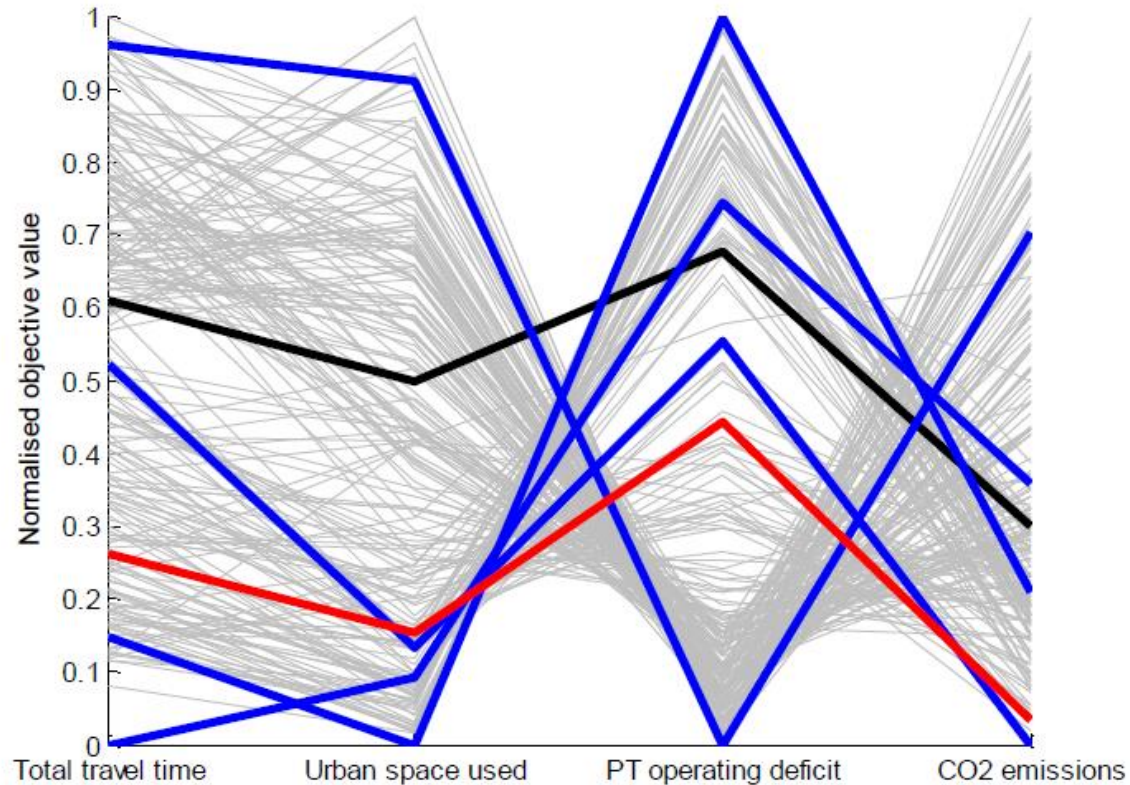




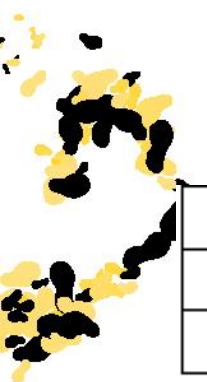
# Best value per objective



*Black: base situation*  
*Blue: individually optimal solutions*  
*Red: best simultaneous improvement for all four objectives: 0.4% w.r.t. base*



Base situation	250007	68720	-36594	1352
Minimum	248034	67659	-56203	1346
Improvement w.r.t. base	-0.79%	-1.54%	-6.19%	-0.45%

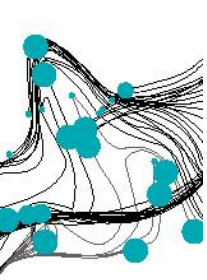




## Resolution of measures

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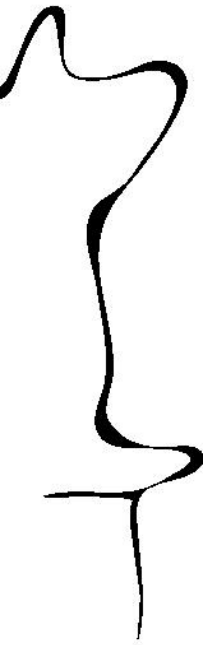
- Selected measures all related to multimodal trip making
- Small relative improvements, but considerable absolute improvements
- Every AM peak
  - 4000 hours of travel time
  - 2000 parked cars
  - 12 tons of CO<sub>2</sub> emissions
    - Equivalent to the daily direct CO<sub>2</sub> emissions of 500 Dutch households

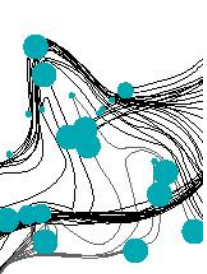


## Relations between objectives

- Correlation between objectives

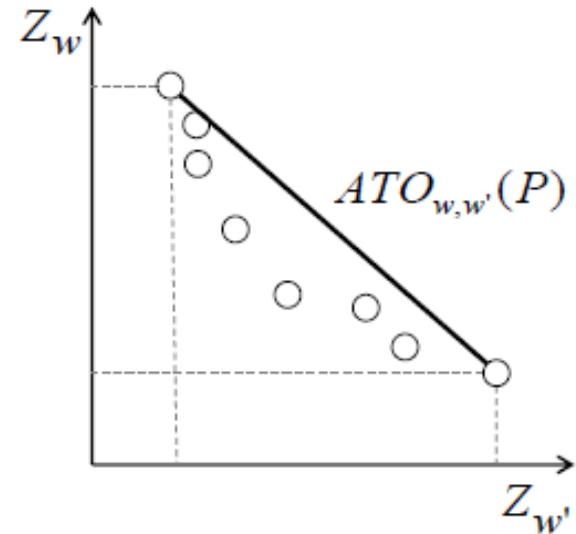
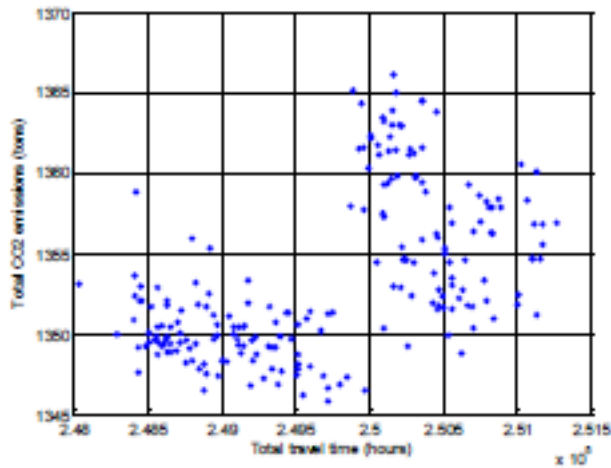
	TTT	USU	OpD	CE
Total travel time (TTT)	1.00	0.79	-0.87	0.53
Urban space used (USU)	0.79	1.00	-0.87	0.84
Operating deficit (OpD)	-0.87	-0.87	1.00	-0.62
CO <sub>2</sub> emissions (CE)	0.53	0.84	-0.62	1.00





# Relations between objectives

- Average trade-off values



$w \setminus w'$	TTT (hours)	USU (# of cars)	OpD (euros)	CE (kilos)
TTT (hours)		-2.44	-0.144	-0.232
USU (# of cars)	-0.411		-0.067	-0.0661
OpD (euros)	-6.94	-14.9		-1.12
CE (kilos)	-4.31	-15.1	-0.89	



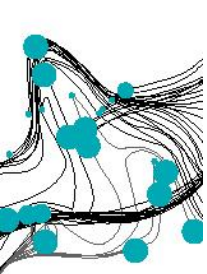
## Relations between decision variables and objectives

- Correlation between types of decision variables and objectives

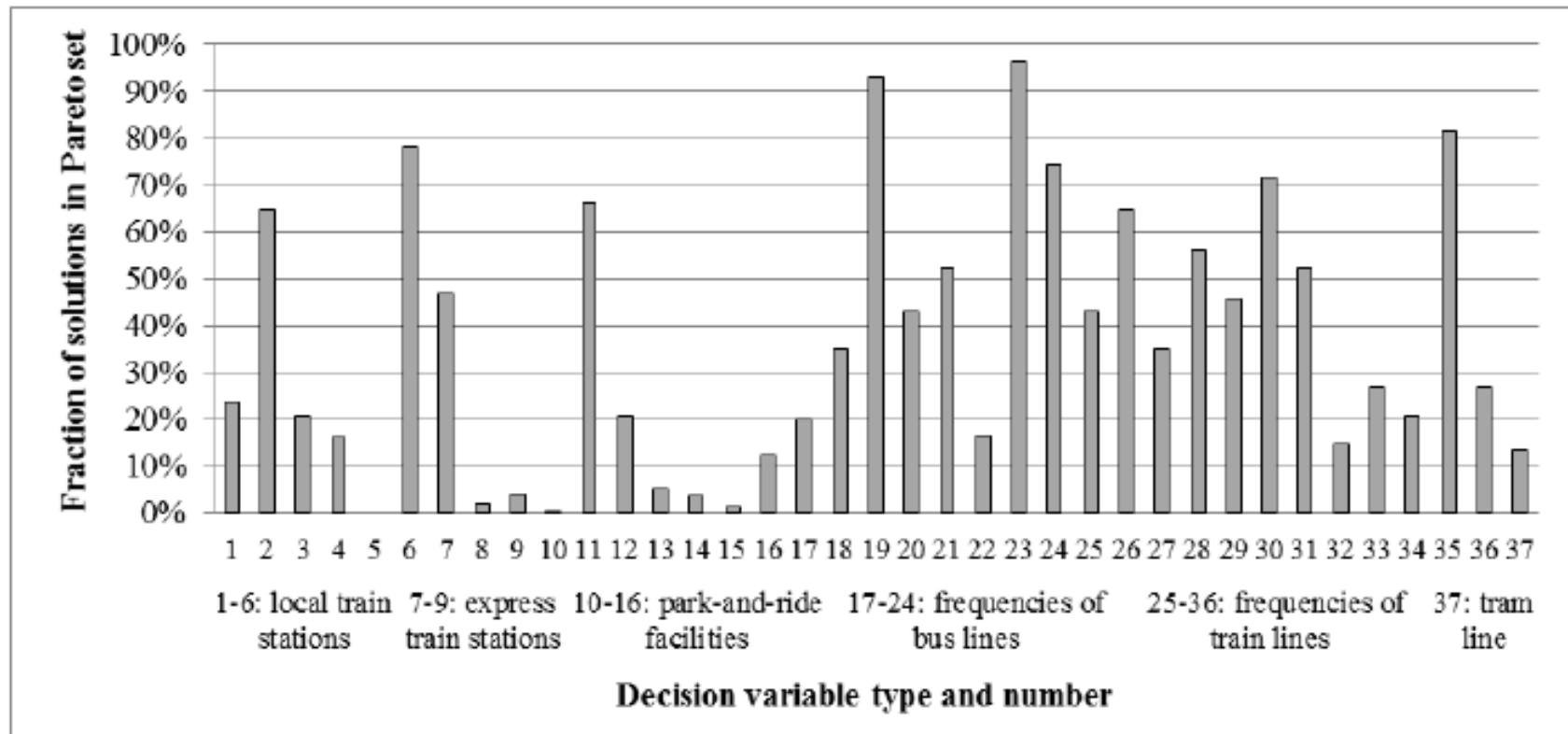
	TTT	USU	OpD	CE
Train stations	-0.50	-0.63	0.57	-0.41
Express train stations	0.32	0.23	-0.30	-0.04
P&R facilities	-0.43	-0.36	0.47	-0.16
Bus frequencies	-0.71	-0.80	0.77	-0.57
Train frequencies	-0.85	-0.93	0.96	-0.78

- Correlation between types of decision variables

	Train stations	Express train stations	P&R facilities	Bus frequencies	Train frequencies
Train stations	1.00	-0.12	0.25	0.52	0.55
Express train stations	-0.12	1.00	-0.19	-0.21	-0.25
P&R facilities	0.25	-0.19	1.00	0.30	0.42
Bus frequencies	0.52	-0.21	0.30	1.00	0.73
Train frequencies	0.55	-0.25	0.42	0.73	1.00



# Percentage of active decision variables in Pareto set



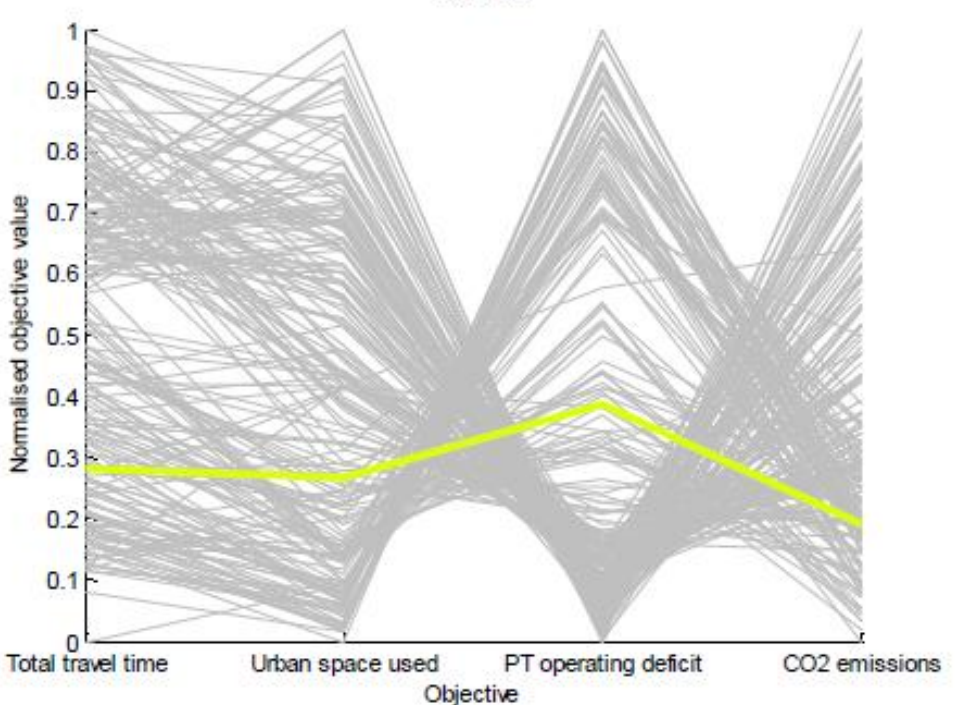
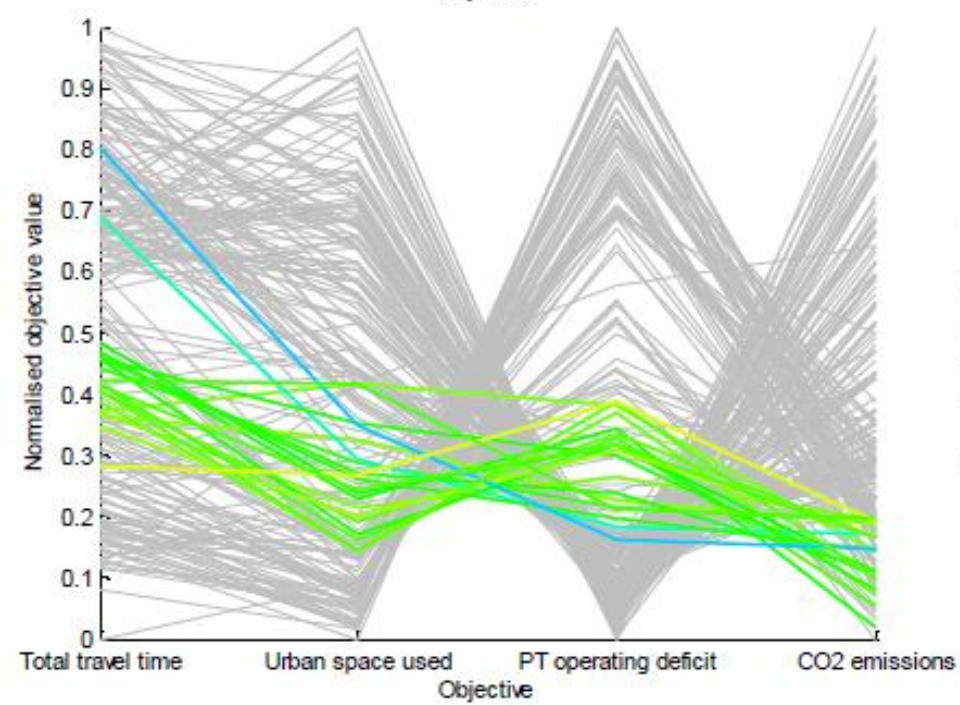
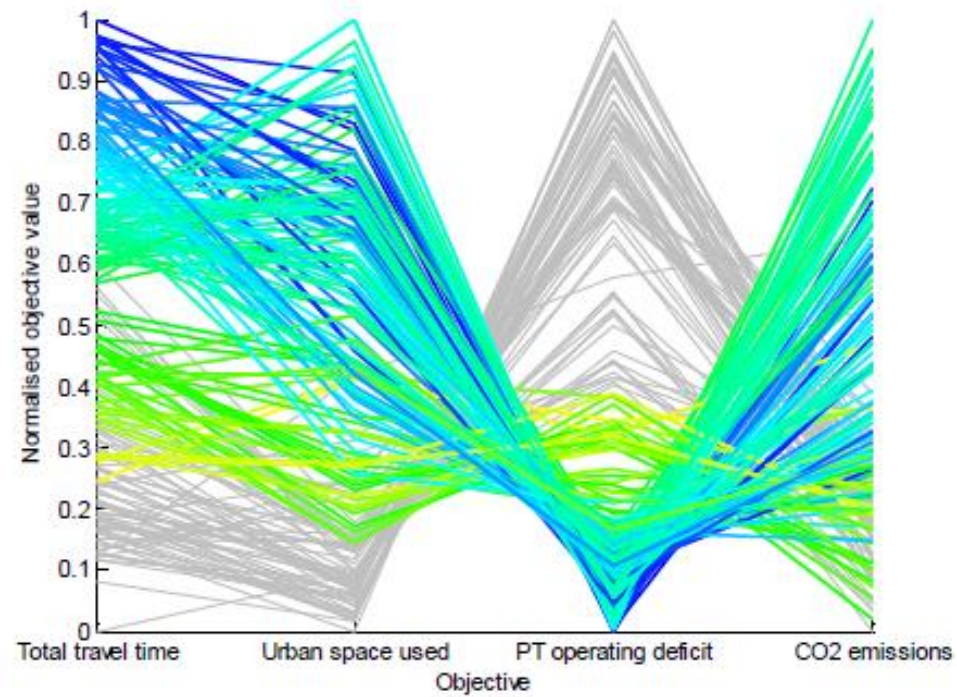
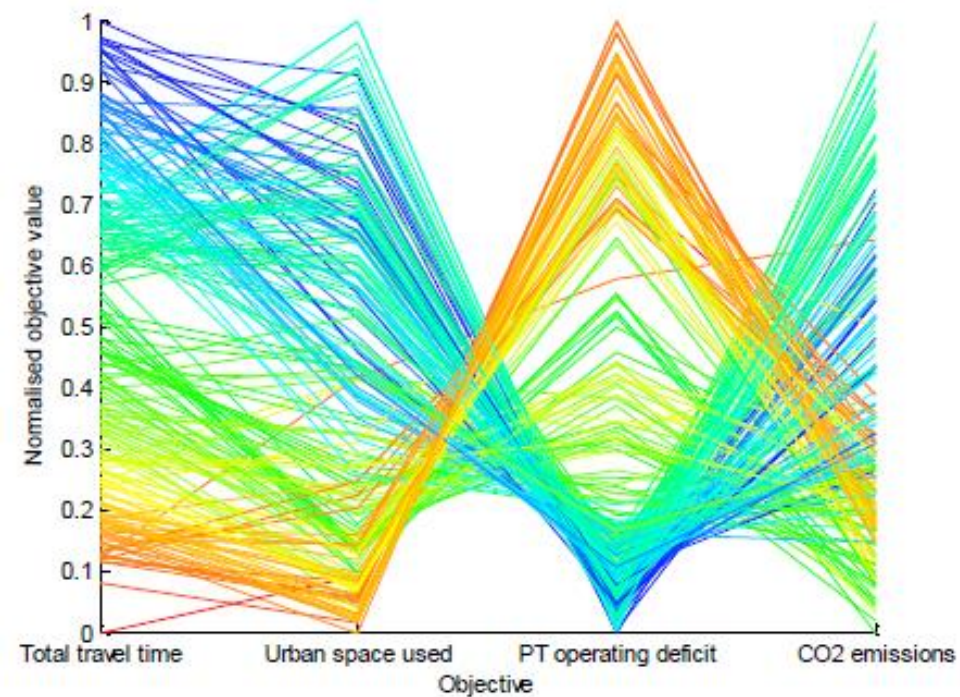


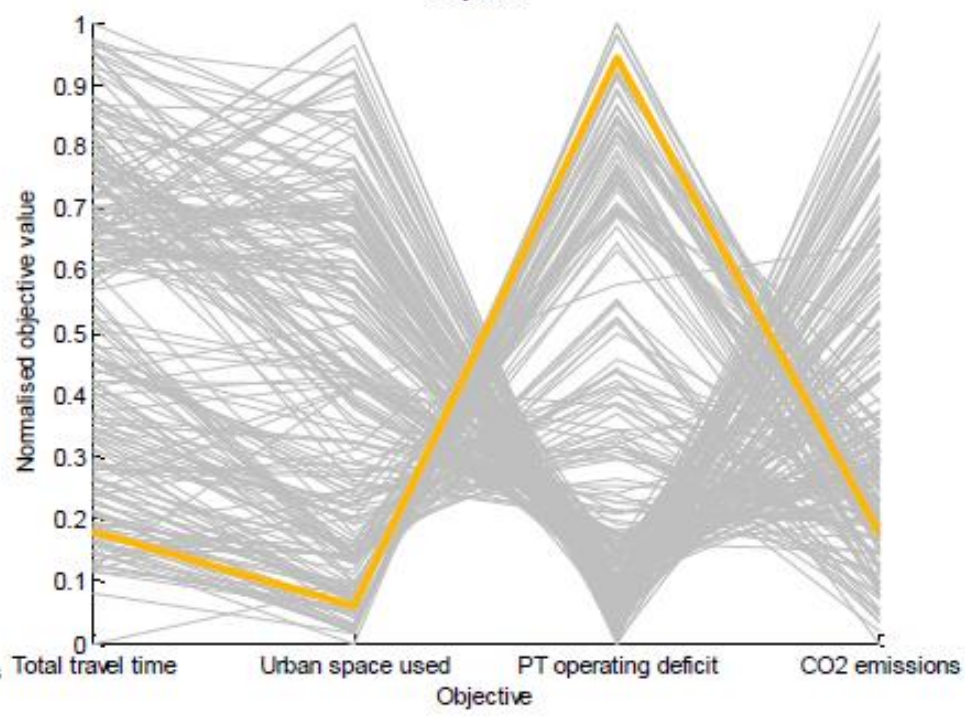
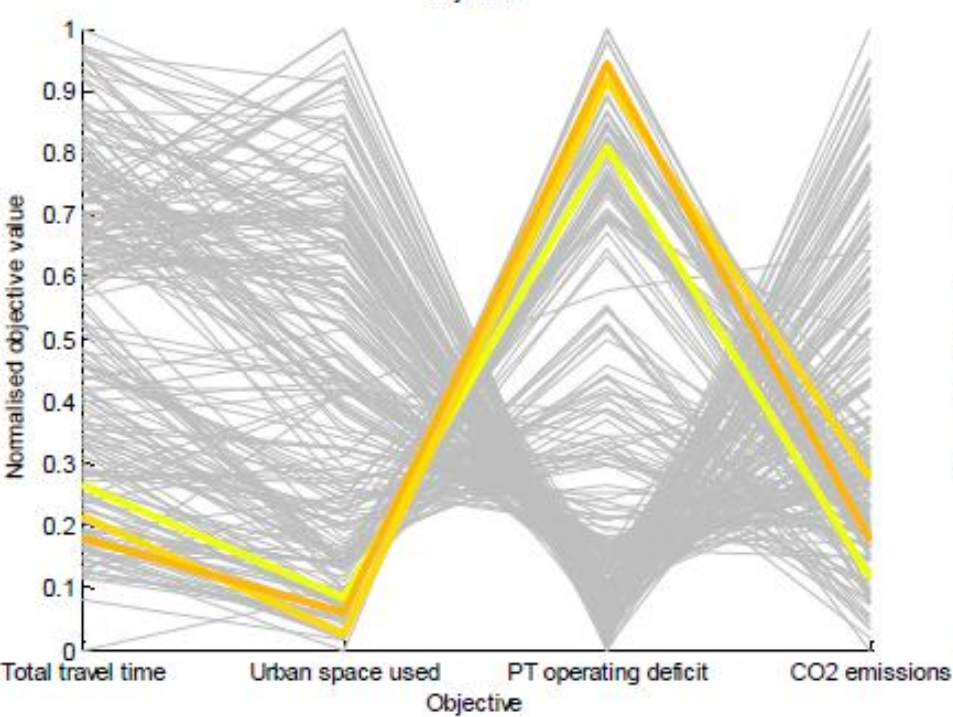
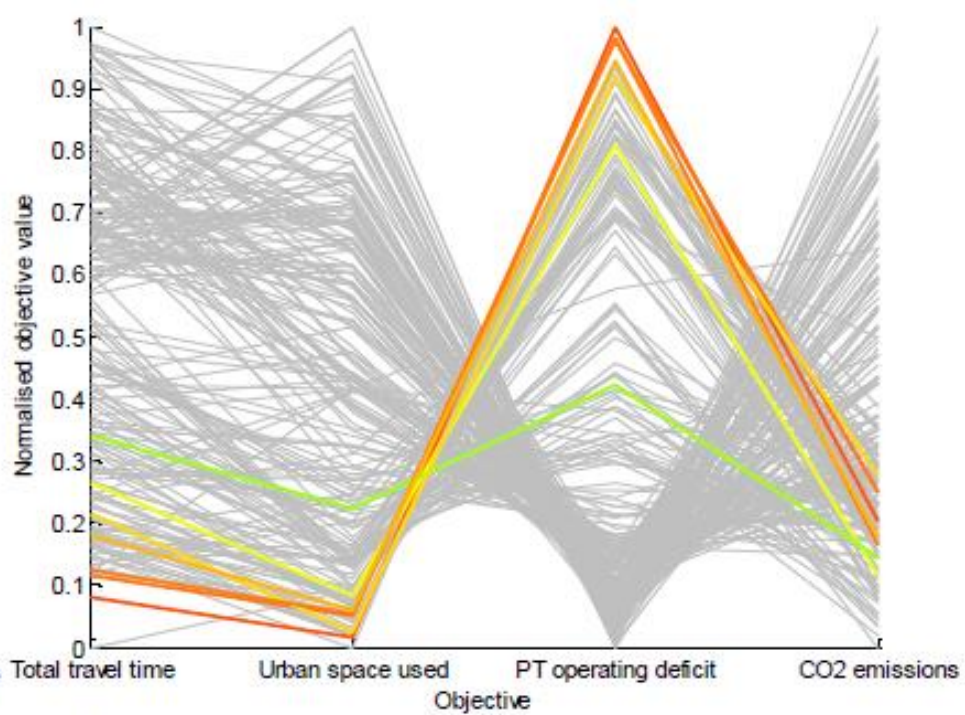
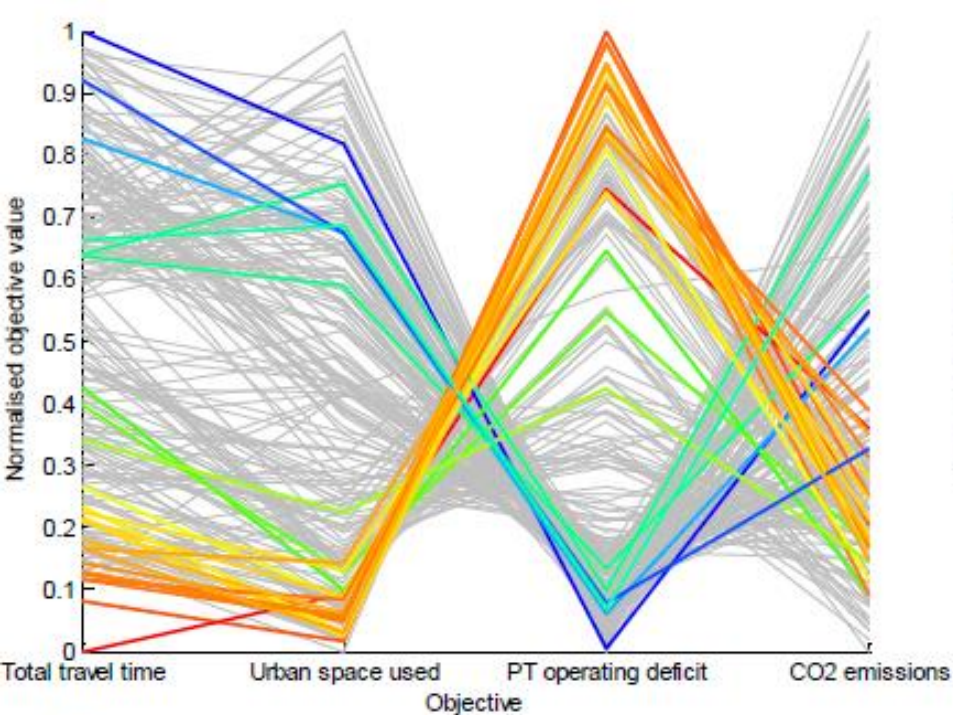


## Step-by-step pruning

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- A post-optimisation method to reduce the number of solutions in the Pareto set step-by-step to come to a final solution for implementation
- Method is based on interviews with policy officers in The Netherlands
- Putting additional constraints to objective values
- Fixing certain decision variables, i.e. choosing a certain measure
  - Often political desires exist that are not included in the objective values







## Choosing one solution as a compromise

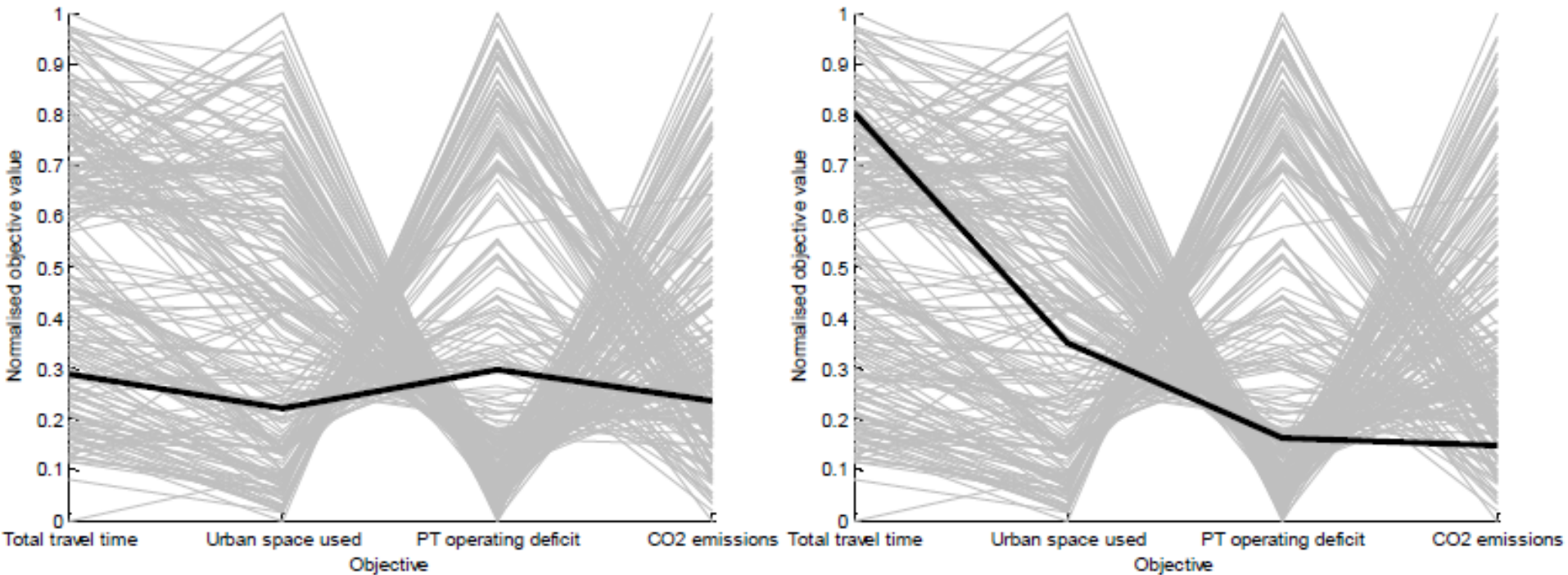
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- A post-optimisation method to reduce the number of solutions in the Pareto set step-by-step to come to a final solution for implementation
- Assume each objective represents one political party
- In negotiation, no party will accept a solution with a very bad score
- → the least scoring objective is leading when choosing a compromise solution
- The min-max solution:

$$BCS_{W_C}(P) = \operatorname{argmin}_{\underline{y} \in P} \left( \max_{w \in W_C} \overline{Z}_w(\underline{y}) \right)$$

- Objective set  $W_C$  may contain all objectives, or a subset of objectives

# Best compromise solution: min-max solution





# Conclusions

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- Methodology development
  - The Pareto set enables an interactive process to demonstrate consequences of certain choices directly
  - Trade-offs between objectives are seen as marginal costs, to judge whether additional investments are worthwhile
    - Visualise in scatterplot
  - Step-by-step pruning to come to a final decision
    - Visualise in parallel coordinate plot
  - Min-max solution as best compromise solution
    - Visualise in parallel coordinate plot



## Conclusions

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- Multimodal passenger NDP: case study in the Randstad
  - Small relative improvements, but considerable absolute improvements
  - A reduction of 0.4% is possible for all four objectives simultaneously
  - It is possible to satisfy all four objectives simultaneously to a large extent
  - Increasing frequencies in general is more effective than opening new train stations and park-and-ride facilities
  - In the case bus routes are in general complementary to train routes rather than competitive



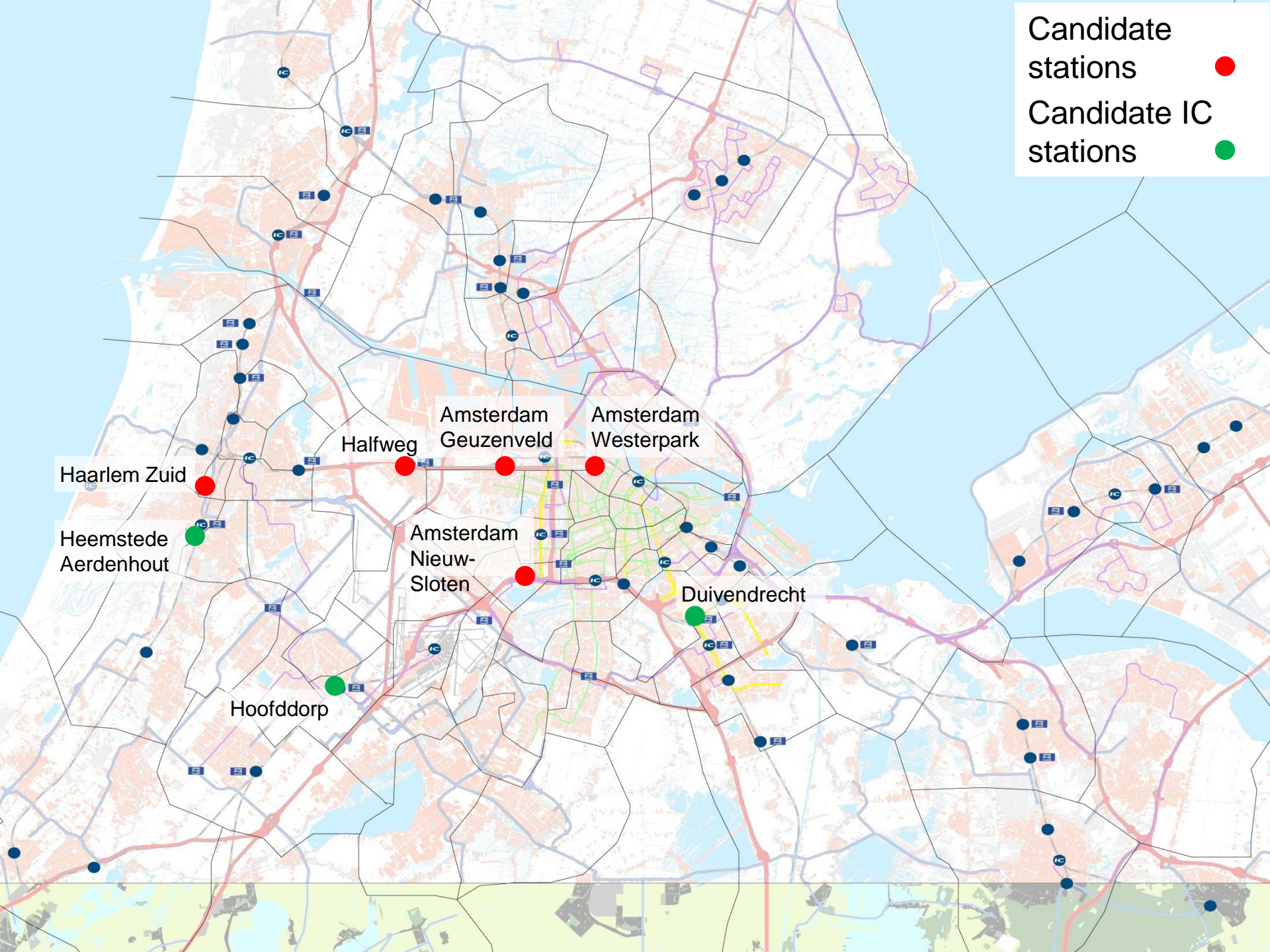
## Further information

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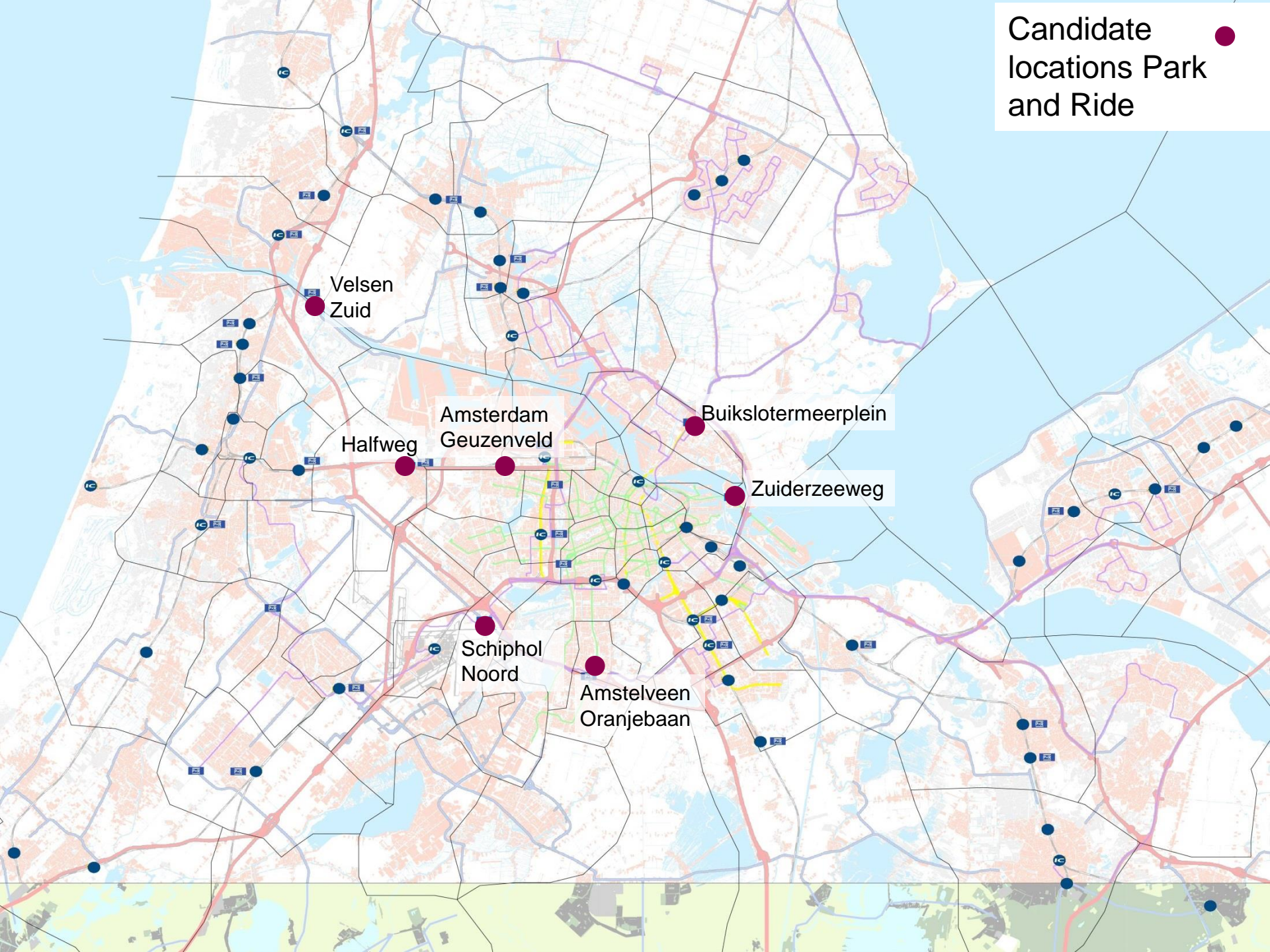
- Full paper included in conference proceedings
- Public defense at University of Twente: 15<sup>th</sup> of October, 14:45 PM
- Contact information [tbrands@goudappel.nl](mailto:tbrands@goudappel.nl)
- Funding:
  - NWO (The Netherlands Organisation for Scientific Research)
  - program Sustainable Accessibility of the Randstad (SAR / DBR)
  - project Sustainable and Reliable Multimodal Transportation networks (SRMT)
  - See <http://dbr.verdus.nl/pagina.asp?id=717>



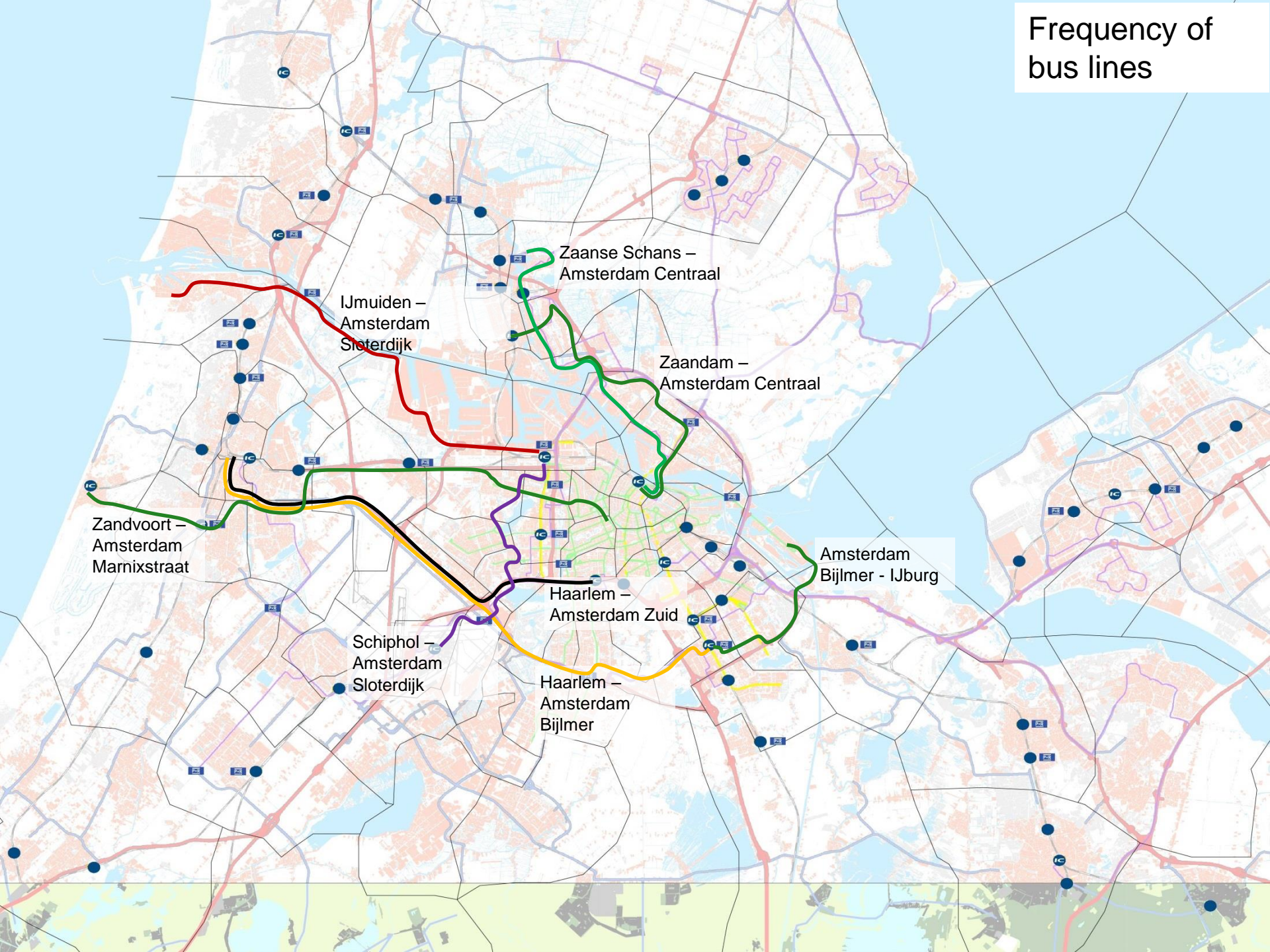
Candidate stations ●  
Candidate IC stations ●



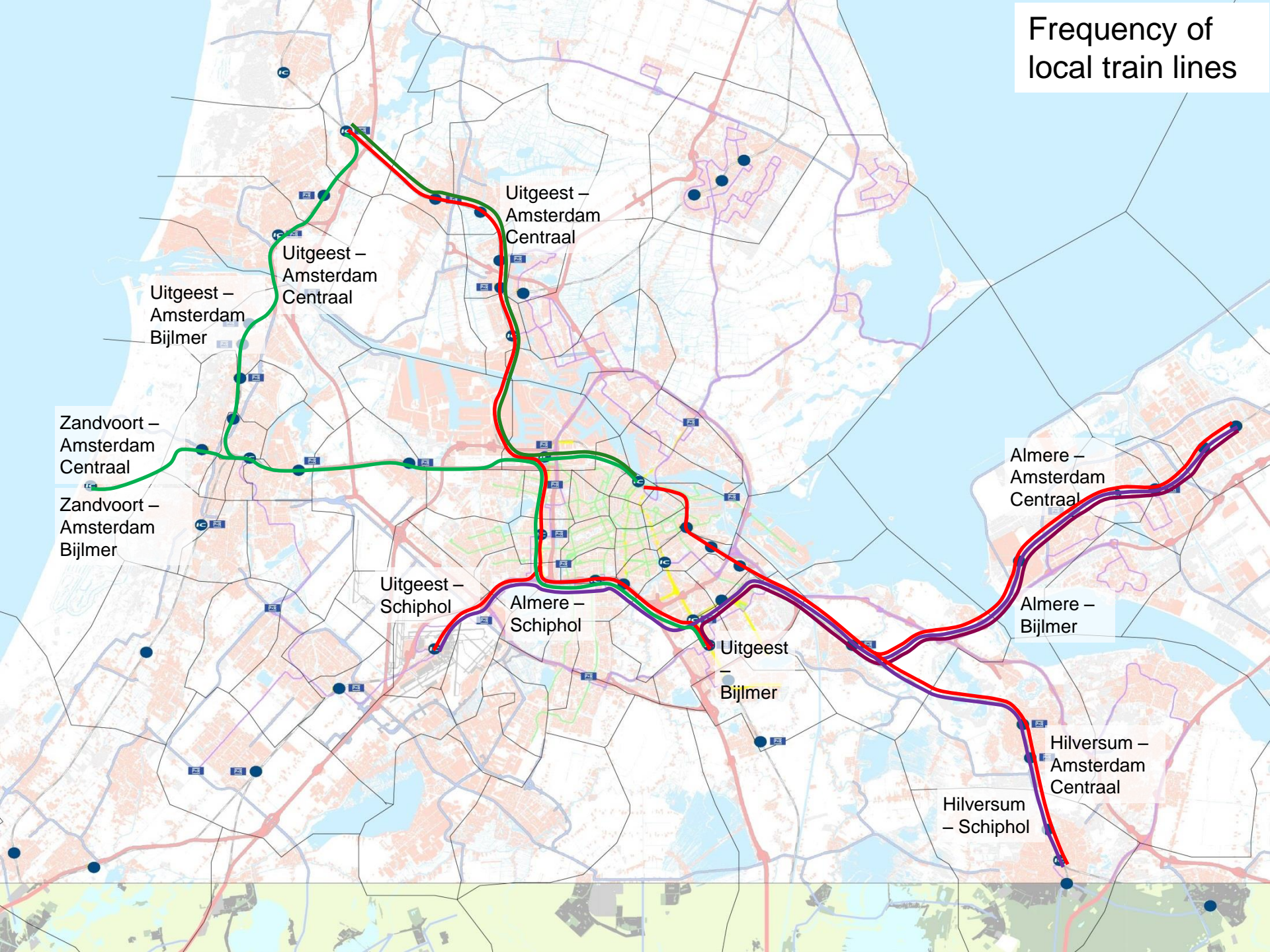
Candidate  
locations Park  
and Ride



# Frequency of bus lines



# Frequency of local train lines



<i>Decision variable type</i>	<i>Decision variable</i>	<i>Decision variable name</i>	<i>Real value in base solution</i>
Opening / closure of train station	$y_1$	Halfweg-Zwanenburg	1
	$y_2$	Haarlem Zuid	0
	$y_3$	Amsterdam Geuzenveld	0
	$y_4$	Amsterdam Nieuw Sloten direction East	0
	$y_5$	Amsterdam Nieuw Sloten direction North	0
	$y_6$	Amsterdam Westerpark	0
Express train status of train station	$y_7$	Hoofddorp	0
	$y_8$	Duivendrecht	1
	$y_9$	Heemstede-Aardenhout	1
Opening / closure of P&R facility	$y_{10}$	Train station Halfweg-Zwanenburg	0
	$y_{11}$	Velsen South	0
	$y_{12}$	Amsterdam, Zuiderzeeweg	0
	$y_{13}$	Train station Geuzenveld	0
	$y_{14}$	Amsterdam, Buikslotermeerplein	0
	$y_{15}$	Amstelveen, Oranjebaan	0
Frequency of bus line	$y_{16}$	Schiphol North	0
	$y_{17}$	Haarlem - Amsterdam South	8
	$y_{18}$	Haarlem - Amsterdam Bijlmer	4
	$y_{19}$	Ijmuiden - Amsterdam Sloterdijk	2
	$y_{20}$	Zandvoort - Amsterdam Marnixstraat	2
	$y_{21}$	Zaanse Schans - Amsterdam Centraal	8
	$y_{22}$	Zaandam - Amsterdam Centraal	8
	$y_{23}$	Schiphol - Amsterdam Sloterdijk	0
Frequency of local train line	$y_{24}$	Amsterdam Bijlmer – IJburg	8
	$y_{25}$	Uitgeest - Amsterdam Centraal	2
	$y_{26}$	Uitgeest - Schiphol - Hoofddorp	0
	$y_{27}$	Uitgeest - Zaandam - Zuid - Bijlmer	0
	$y_{28}$	Zandvoort - Haarlem - Zuid - Bijlmer	0
	$y_{29}$	Uitgeest - Haarlem - Zuid - Bijlmer	0
	$y_{30}$	Zandvoort - Haarlem - Centraal	2
	$y_{31}$	Uitgeest - Haarlem – Centraal	2
	$y_{32}$	Amsterdam Centraal - Almere Oostvaarders	2
	$y_{33}$	Hoofddorp - Almere Oostvaarders	4
	$y_{34}$	Bijlmer - Almere Oostvaarders	0
	$y_{35}$	Utrecht - Hilversum - Amsterdam Centraal	4
	$y_{36}$	Utrecht - Hilversum - Hoofddorp	2
Extension of a tram line	$y_{37}$	Amsterdam Geuzenveld	0